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# Number Sense Test Round 11424

	e:		
	e: ol:		
	place ID sticker inside this box	Correct: Incorrect:	(Remember, Correct and Incorrect must
1.	6 + 12 =	18. $72 \times 15 =$	
2.	19 - 9 =		even numbers between
	25 + 18 =		× 14 =
	34 - 16 = $8 \times 9 = $	21. $363 \times 11 = $	
6.	$42 \div 7 = \_\_\_$		189 is
7.	What is the the thousands digit of 18436?		
8.	14 × 11 =	25. 7 nickels $+$ 7 per	nnies = $(cents)$ .
9.	What is the remainder of $242 \div 7?$	26. $53 \times 57 =$	
10.	(estimate) $115 + 456 + 223 = $	27. $\frac{3}{4} \times \frac{28}{15} = $	(fraction).
11.	$4 \times 1 + 3 \times 100 + 9 \times 1000 = $		of the primes between
	Round 27.65(whole number).		
13.	CXXI = (Arabic Numerals).		
14.	123 + 49 =	. ,	=
15.	$23 \times 12 =$	31. 6 feet $=$	inches.
16.	$16 \times 25 =$	32. $\frac{1}{2} + \frac{3}{4} = $	(decimal).
17.	$189 \div 3 = \_\_\$	33. If $x = 16$ , $\sqrt{x} + 2$	$2x^2 = \underline{\qquad}.$

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- 34. One egg costs 7 cents. A dozen eggs cost \_\_\_\_\_ cents.
- 35.  $84 \times .25 =$  \_\_\_\_\_\_.
- 36. 40% =\_\_\_\_(fraction).
- 37.  $704 \div$  \_\_\_\_\_\_= 64.
- 38.  $26^2 =$ \_\_\_\_\_.
- 39. LCM of 21 and 12 = \_\_\_\_\_.
- 40. (estimate)  $135 \times 7 =$  \_\_\_\_\_.
- 41. What is the area of a square with side length 35? \_\_\_\_\_.
- 42. What is the average value of the numbers 12, 5, 6 and 9? \_\_\_\_\_.
- 43.  $.12 \times 18 =$ \_\_\_\_(decimal).
- 44.  $4 + 12 = 8 \times$  \_\_\_\_\_\_.
- 45. If a = 3, then 27a + 4 = \_\_\_\_\_.
- 46.  $1 + 3 + 5 + \dots + 23 =$ \_\_\_\_\_.
- 47.  $\sqrt{81} =$ \_\_\_\_\_.
- 48. What is the perimeter of a square with side length 27? \_\_\_\_\_.
- 49.  $110011_2 =$ \_\_\_\_(base 4).
- 50. (estimate)  $5\pi^2 =$  \_\_\_\_\_.
- 51.  $\frac{3}{7} \times \frac{14}{15} =$  \_\_\_\_\_(fraction).
- 52. What is the length of the hypotenuse of a triangle with legs 6 and 8? \_\_\_\_\_.
- 53.  $\sqrt[3]{343} =$ \_\_\_\_\_.
- 54. What is the volume of a cube with side length 8? \_\_\_\_\_.
- 55. 37.5% =\_\_\_\_\_(fraction).
- 56. If a rectangle's perimeter is 64 and its length is 19, then its width is \_\_\_\_\_.

57.	$346_7 = \{10}$ .
58.	$\sqrt{729} = \underline{\qquad}$
59.	If a circle's radius is 13, its area is
60.	(estimate) $7^5 =$
61.	$125^2 - 75^2 = $
62.	If the angles of a triangle are $34^{\circ}$ , $75^{\circ}$ and $x^{\circ}$ , $x^{\circ} =$
63.	$1^2 + 3^2 + 5^2 + 7^2 + 9^2 = \underline{\qquad}$
64.	7643 + 642 - 726 =
65.	The area of a triangle with side lengths 5, 5 and 6 is
66.	$77^2 = $
67.	24% of $120 = $ (decimal).
68.	The area of a rhombus with diagonals $12 \text{ and } 13 = $
69.	If $\$1 = 11.2$ Rands, $\$75 = $ (Rands).
70.	(estimate) $3061^2 = $
71.	$94 \times 107 =$
72.	A regular dodecagon has <u>diagonals</u> .
73.	170 out of $250 = $ %.
74.	$2050^2 = $
75.	$845 \div 15 = $ (mixed number).
76.	$391 \div 23 = $
77.	$2.4 \times 56 = $ (decimal).
78.	$\frac{3}{8} \times 65 = $ (mixed number).
79.	Rolls are sold for 72¢ a dozen. How much would 43 rolls cost? $(c)$ .
80.	(estimate) $364000 \div 47$

Number Sense Test

Round 11424

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### mathleague.org Sprint Round Answer Sheet

If you have been given an ID sticker,	Students, follow us on twitter! http://twitter.com/mathleague	# Correct x (4) =
please place it in this box with the QR code to the left.	email address:	# Incorrect $x(-1) = $
	(only if you are over 13 and want to be added to our mailing list)	SCORE = DOUBLE CHECK = Students: don't write in this box
Name: G	rade: School:	

#### Instructions

This test consists of thirty multiple-choice questions. High school students will be given one hour to respond to as many as possible; elementary students will be given forty minutes. No calculators are allowed on this test. Please mark all responses on this answer sheet by completely filling in the bubble corresponding to your chosen answer. You may make notes and computations on the test pages, but only answers indicated on this answer sheet will be graded for credit. If this test is a qualifying round and you achieve a high enough score, you will be invited to the state championship later in the year; see our website for details.

#### Scoring

Four points will be awarded for each correct answer, and one point will be deducted for each incorrect answer. No points will be awarded or subtracted for questions left unanswered. Any question with two answers indicated will be counted as incorrect. Please keep in mind that, even though the questions may progress in difficulty toward the end of the test, no bonus points are awarded for solving problems that seem especially difficult.

### Quality Control

Please email us any compliments, complaints, or comments about the contest you attended. Our email address is mathleague@mathleague.org. Remember that only contests listed on the website are officially sanctioned mathleague.org meets.

- 1. В С D Е 2. В С D 3. В С D Е В С D Е 4 В С D Е 5. В С D Е 6. В D Е С 7. В Е 8 С D В С D Е 9 В С D 10.
- 11. В С D Е 12. В С D E 13. В С D Е A
- 14. (A) (B) (C) (D) (E)
- 15. A B C D E
- 16.  $(A \otimes C) \otimes (D \otimes E)$
- 17. (A) (B) (C) (D) (E)
- 18. (A) (B) (C) (D) (E)
- 19. (A) (B) (C) (D) (E)
- 20. A B C D E
- 21. В С D Е 22. В С D Е 23. В С D Е В С D Е 24. В С D Е 25. 26. В D Е C В D Е 27. С В D 28. С Е
- 29. (A) (B) (C) (D) (E)
- 30. A B C D E



A) 45%

B) 49%

- 1. Compute the value of 123 + 456. A) 789 B) 567 C) 678 D) 579 E) Other 2. What is the mode of the set  $\{1,2,3,4,4,4,5,5,6\}$ ? B) 5 C) 6 D) 3 A) 9 E) Other 3. Compute  $340 \div 17$ . B) 15 C) 12 D) 16 E) Other A) 25 4. Compute  $13^3$ . A) 2197 B) 1897 C) 920 D) 2341 E) Other 5. Jamal has three books. They have 367, 295, and 488 pages, repectively. If Jamal reads 25 pages a week, how many weeks will it take him to finish all three books? A) 42 B) 46 C) 52 D) 60 E) Other 6. Compute  $45 \times 6 + 97 \times 5$ . A) 650 B) 890 C) 675 D) 755 E) Other 7. Jeffrey makes coffee for his 9 colleagues, and one of his collegues asks for half sugar. Once all the coffee was made, Jeffrey forgot which one had half sugar. What is the probability of him choosing the right mug? Express your answer as a common fraction. A)  $\frac{2}{3}$ B)  $\frac{1}{6}$ C)  $\frac{1}{3}$ D)  $\frac{1}{9}$ E) Other 8. A right triangle has side lengths 6cm, 9cm, and xcm. What is the largest possible value of x? B)  $4\sqrt{7}$ C)  $3\sqrt{13}$ D)  $3\sqrt{11}$ A)  $4\sqrt{19}$ E) Other 9. Amy drinks 1.5L of milk every weekday, but 1L each weekend day. Every Wednesday, Amy gives her cat a 300mL bowl of milk. How many liters (L) of milk will Amy use over 26 weeks? A) 292.6 B) 211.3 C) 179.6 D) 254.8 E) Other 10. What is the volume of a cube with a side of 6cm? C)  $24 \text{ cm}^{3}$ A)  $216 \text{ cm}^3$ B)  $18 \text{ cm}^3$ D) 194  $cm^3$ E) Other 11. Last year, Lee bought shares with a value of \$15 each. This year the value of the shares dropped to \$9 each. By what percent did the value of the shares decrease?
- 12. A large number of marbles with different numbers on them are placed in a box. Two marbles are chosen WITHOUT replacement (the second marble is chosen from those remaining after the first one is removed). What is the probability that the first marble

D) 35%

E) Other

C) 25%

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has a higher number than the second one?

- B)  $\frac{1}{5}$ D)  $\frac{1}{10}$ A) Cannot be determined without knowing the numbers on the marbles.
- C) Cannot be determined without knowing how many marbles there are.
- E) Other
- 13. A large number of marbles with different numbers on them are placed in a box. Two marbles are chosen WITH replacement (the first marble is returned to the box before the second marble is chosen). What is the probability that the first marble has a higher number than the second one?

A) Cannot be determined without knowing how many marbles there are. B)  $\frac{1}{2}$ C)  $\frac{1}{10}$ D) Cannot be determined without knowing the numbers on the marbles. E) Other

- 14. What is the average of the first 50 positive integers? B) 26 D) 25 E) Other A) 25.5 C) 24.5
- 15. Three consecutive numbers add up to 75. What is the smallest of these numbers? A) 24 B) 25 C) 26 D) 74 E) Other
- 16. Solve for x: 5x + 7 = 2x + 40. B) 33 D) 47 E) Other A) 54 C) 11
- 17. A rectangle with diagonal of length 13cm has width 12cm. What is the length of the rectangle? C)  $\sqrt{313}$ D) 12 E) Other A) 5 B) 25
- 18. How many elements are in the intersection of the set  $\{1,4,7,10,\ldots,61\}$  and the set  $\{1,6,11,16,\ldots,61\}$ ? A) 6 B) 3 C) 2 D) 5 E) Other
- 19. You and your friends order pizza from a delivery service. There are 8 different bases, 18 different toppings and 6 different cheeses. How many different pizzas can you have that consist of one base, one topping, and one cheese? B) 643 C) 792 D) 839 E) Other A) 812
- 20. Mike has 8 cats. If one of his cats runs away, what percentage his cats have run away? A) 12.5 % B) 25% D) 18% C) 7.5% E) Other
- 21. An equilateral triangle has side length 18. What's the perimeter of the triangle? A) 36 B) 18 C) 72 D) 54 E) Other
- 22. An equilateral triangle has perimeter 18. What's the side length of the triangle?



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- A) 72 B) 36 C) 6 D) 54 E) Other
- 23. If 2x + 3y = 5 and 4x y = 7, what is the value of 6x + 2y? A) 4 B) 12 C) 9 D) Cannot be determined E) Other
- 24. A rectangular prism has a length of 12cm, width of 7cm, and height of 4cm. If its length, width and height are all doubled, what would the surface area of the prism be?
  A) 640 B) 160 C) 2560 D) 1280 E) Other
- 25. What is the value of  $(7 \times 143 \times 2014)$ ? A) 2018014 B) 2015024 C) 2026014 D) 2016024 E) Other
- 26. Carolyn pretends to be a kangaroo as she hops up and down a number line with both positive and negative numbers. To multiply  $2 \cdot 5$ , she starts at 0, faces in the positive direction, and hops forward by 2s 5 times, ending at 10. To find  $2 \cdot (-5)$ , she starts at 0 facing positive, flips around so she faces in the negative direction, and and hops forward by 2s, ending at -10. To find  $(-2) \cdot (-5)$ , she could start at 0 and then do which of the following?

A) Face negative and hop forward, ending at 10.B) Face positive and hop backward, ending at 10.C) Face negative and hop backward, ending at 10.D) Face negative and hop forward, ending at -10.E) Other

- 27. Refer to the problem above. Akhil tries a decimal number line where clothespins mark numbers in tenths. To make things even more challenging, he chooses a division problem. To find (-2.1) ÷ 0.3, he could do which of the following?
  A) Face positive and hop forwards in increments of 0.3, 7 times, until he reaches -2.1.
  B) Face negative and hop forward in increments of 0.3, 0.7 times, until he reaches -2.1.
  C) Face negative and hop forward in increments of 0.3, 7 times, until he reaches -2.1.
  D) Face negative and hop backward in increments of 0.3, 7 times, until he reaches -2.1.
  E) Other
- 28. Being hospitalized with malaria (a disease caused by mosquito bites) costs \$2000. Uanhenga purchases a mosquito net for \$5. Assuming it prevents him from contracting malaria, what is the return on his investment? Percentage return on investment can be calculated as  $\frac{profit}{investment} \cdot 100$ .

A) 0% B) 39900% C) 40% D) 1995% E) Other

29. Beatrix sets her watch 10 seconds behind the correct time but each day it falls 3 additional seconds behind. How many seconds is her watch currently behind if she set it 36 days ago?

A) 176 B) 181 C) 226 D) 93 E) Other

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30. A picture with a perimeter of 1.2m is framed. One side of the picture is 40cm, and the distance from the edge of the picture to the edge of the frame is 1.5cm on all sides of the picture. What's is the area of the portion of the frame not covered by the picture? Express your answer in cm<sup>2</sup>.

A) 198 B) 189 C) 203 D) 134 E) Other



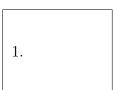




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Grade:
School:

	Score: #1	Scorer's Initials
place ID sticker inside this box	Score: #2	Scorer's Initials

1. Baby Jacqueline is 9 months old. Convert her age to years. Express your answer in decimal form.



2. In Legoworld, a shopowner charges 10 studs for a pair of rocket boots. The greedy king insists on a 30% tax on all sales. A lego minifigure wants to buy the boots. How many total studs (price plus tax) should he pay?

2.	
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3. Qiao is trying to do her homework. The first hour, her little brother interrupts her 3 times. The next hour, her little brother interrupts her 11 times. The third hour, her little brother interrupts 4 times. How many times per hour is she interrupted on average? 3.

4. A standard six-sided die is rolled onto a table. The product of the visible numbers is 144. What is the number on the bottom side of the die?

4.
----







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	School:

	Score: #5 Scorer's Initials
place ID sticker inside this box	Score: #6 Scorer's Initials

5. Dexter builds a hollow shelter in Minecraft using blocks. Assume each block is a cube measuring 1 unit  $\cdot$  1 unit  $\cdot$  1 unit. His shelter is 6 blocks wide by 8 blocks long by 4 blocks tall and 1 block thick. What is the exterior surface area of his structure?

5.

6. Refer to the problem above. What is the interior surface area of Dexter's shelter?

6.







<b>.</b>	Name:
<u>197. in</u> 1	Grade:
	School:

	Score: #7 Scorer's Initials
place ID sticker inside this box	Score: #8 Scorer's Initials

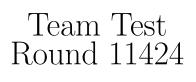
7. What is the perimeter of a regular decagon with side length 8?



8. A standard six-sided die is rolled twice. What is the probability that the value of the second die is higher than that of the first? Express your answer as a common fraction.

8.	



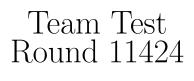




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1.	2	2.	3.		4.		5.	
6.	7	7.	8.		9.		10.	

Team Test - Round 11424 -  $\bigodot$  2014 mathleague.org







- 1. Bob loves to eat apples. He ate 3 apples on Monday, 4 apples on Tuesday, and 8 apples on Wednesday. How many total apples did Bob eat those three days?
- 2. Natsu, Gray, Erza, and Lucy are in a running race. None of them tied each other. Natsu finished after Erza but before Gray. Lucy finished behind Natsu. Who finished second?
- 3. Old McDonald had a farm, on his farm he had sheep and ostriches. If there were a total of 37 heads and 120 feet on the farm, how many ostriches did he have? Remember, each animal has one head, and ostriches have two feet while sheep have four feet.
- 4. Diego's father is 5 times Diego's age. Two years ago he was six times Diego's age. How old is Diego?
- 5. Yesterday, Chef Ramsey used 44 eggs to make 6 Malva Puddings and 8 Lemon Meringues. Today, he used 52 eggs to make 6 Malva Puddings and 10 Lemon Meringues. How many eggs does it take to make a Malva Pudding?
- 6. Captain Liz wants to get her ship's cargo of yogurt from the east side of the Panama Canal to California before it gets too old to sell. Unfortunately, there is a long line of ships waiting to use the canal, and each day 40 ships are let into the canal at the beginning of the day and take all day to transit the canal. If Captain Liz can use the shortcut, it will take one day to transit the canal and another two days to get to California. If she must go around South America, the total trip will take Captain Liz 7.5 days. What is the maximum number of ships that can be in line in front of Captain Liz when the canal opens on the first day such that it still makes sense for her to use the canal?
- 7. A community group in South Carolina decides to buy a decommissioned battleship. (Decommissioned means that it is no longer in use and the weapons have been removed.) The ship costs \$5000000, but the buyers have a coupon for 40% off and another 10% off the reduced price. How many more dollars would they save if they instead had a coupon for 50% off the original price?
- 8. Commander Jerjerrod estimates that it will take another 150000 robot-hours to complete the Death Star, but, under pressure, he promises to meet a ridiculous deadline. Assume the deadline is 2 days away and he has 2000 robots available. How many hours would each robot need to work per day in order to have everything completed in time?
- 9. Bag A contains only red marbles, and bag B contains only blue marbles. If David takes 2 marbles out of Bag B and puts them in Bag A, there will be twice as many red







marbles as blue marbles in Bag A. If instead David takes 3 marbles out of Bag A and puts them in Bag B, there will be the same number of red and blue marbles in Bag B. How many total marbles do the two bags contain?

10. In a list of seven distinct positive integers, the mean and median are both seven. What is the largest integer that can appear on the list?